

# Exercise sheet for Session 3

## Uncertain data management

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### 1 Exercise 1: Codd tables

Consider the following instance  $I$ :

Events				Class		Exam	
class	session	teacher	room	class	session	class	session
UDM	1	NULL	NULL	UDM	1	UDM	9
FOO	NULL	NULL	C42	FOO	NULL	FOO	NULL
UDM	9	NULL	NULL				
FOO	NULL	NULL	C43				

**Question 1.** Rephrase in plain English what we know about the UDM class, and what we know about the FOO class.

**Question 2.** Write a Boolean conjunctive query that asks whether some class has a scheduled session in the same room as the exam for that class. Write it in the relational algebra and in the relational calculus.

**Question 3.** Is this query *possible* on the instance? If yes, what is a witnessing possible world?

**Question 4.** Is this query *certain* on the instance? If no, what is a counterexample possible world?

**Question 5.** Write a tuple-generating dependency that says that whenever a class has a scheduled session then it has a scheduled exam with the same teacher (but possibly in a different room).

**Question 6.** Is there a possible world that satisfies this constraint? Do all possible worlds satisfy this constraint?

**Question 7.** Replace three pairs of NULLs by named NULLs to obtain a v-table where the constraint is always respected.

### 2 Exercise 2: v-tables and c-tables

Consider the following instance of a v-table:

Events			
class	session	teacher	room
UDM	1	NULL <sub>1</sub>	NULL <sub>2</sub>
NULL <sub>3</sub>	2	NULL <sub>1</sub>	NULL <sub>4</sub>
FOO	1	John	NULL <sub>2</sub>

**Question 1.** What is this relation saying in plain English?

**Question 2.** Write a query  $Q_1$  in the relational algebra that returns the triples of a class  $class$  and two sessions  $s_1 < s_2$  such that  $s_1$  and  $s_2$  are sessions of  $class$  that have the same teacher.

**Question 3.** Evaluate  $Q_1$  on the instance to obtain a c-table  $R_1$ .

**Question 4.** Write an analogous query  $Q_2$  that returns the triples of a class and two sessions  $s_1 < s_2$  of the class that take place in the same room (but may have different teachers).

**Question 5.** Evaluate  $Q_2$  on the instance to obtain a c-table  $R_2$ .

**Question 6.** Compute a c-table representation of the union  $R$  of  $R_1$  and  $R_2$ .

**Question 7.** How many rows may the possible worlds of  $R$  have?

### 3 Exercise 3: Boolean c-tables

Consider the following instance:

Classes			
session	date	prof	room
2	Nov 28	Antoine	C017
3	Dec 5	Antoine	C47
4	Dec 12	Silviu	C47
5	Jan 9	Silviu	C47
6	Jan 16	Silviu	C47

Consider the following uncertain Boolean events:

- $x_1$ : Room C47 collapses. All UDM classes in room C47 must be canceled.
- $x_2$ : D&K students accept to return from vacation. If this does *not* happen, all UDM classes in January are cancelled.
- $x_3$ : Silviu wins the lottery and escapes to the Bahamas. All of Silviu's classes must be canceled.

**Question 1.** Annotate the rows of the instance to make a Boolean c-table that describes the correct outcome depending on the value of the events.

**Question 2.** How many possible worlds does the table have?

**Question 3.** Using only two Boolean variables  $x$  and  $y$ , create a different Boolean c-table on the same rows that describes the same set of possible outcomes.