

# Uncertain Data Management

## NULLs

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# NULLS

Represent **missing information** in a relation.

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Represent **missing information** in a relation.

Book

<b>date</b>	<b>teacher</b>	<b>class</b>	<b>room</b>
2015-11-23	Antoine	UDM	C47
2015-11-30	Antoine	UDM	C017
2015-12-07	Antoine	UDM	NULL
2015-12-14	NULL	UDM	NULL

# NULLs

Represent **missing information** in a relation.

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**Other name:** Codd tables.

# Semantics

Each **NULL** can be replaced **independently** by **any** domain value

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2015-11-23	Antoine	UDM	C47
2015-11-30	Antoine	UDM	C017
2015-12-07	Antoine	UDM	C42
2015-12-14	Silviu	UDM	C42

# Semantics

Each **NULL** can be replaced **independently** by **any** domain value

## Book

date	teacher	class	room
2015-11-23	Antoine	UDM	C47
2015-11-30	Antoine	UDM	C017
2015-12-07	Antoine	UDM	xbecz
2015-12-14	gruiiik	UDM	buuuk



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SELECT * FROM Book WHERE room='C47';
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How can we evaluate **queries** on Codd tables?

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How can we evaluate **queries** on Codd tables?

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```
SELECT * FROM Book WHERE room='C47';
```

## Book

date	teacher	class	room
2015-11-23	Antoine	UDM	C47

→ **Tricky** semantics, often **criticized!**

# Three-valued logic

- Usually, we evaluate operations as **Boolean**:
  - `WHERE a='42' OR (b=c AND NOT (c=d))`
  - `WHERE False OR (True AND NOT (True))`
  - `False`

# Three-valued logic

- Usually, we evaluate operations as **Boolean**:
  - `WHERE a='42' OR (b=c AND NOT (c=d))`
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- In SQL, values can be **True**, **False**, or **Unknown** (`NULL`)

# Three-valued logic

- Usually, we evaluate operations as **Boolean**:
  - `WHERE a='42' OR (b=c AND NOT (c=d))`
  - `WHERE False OR (True AND NOT (True))`
  - `False`
- In SQL, values can be **True**, **False**, or **Unknown** (`NULL`)
- Essentially **anything** that involves `NULL` is `NULL`

## Three-valued logic (example)

**WHERE** 42=43 **OR** (42=NULL **OR** 42=43)



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**WHERE** 42=43 **OR** (42=NULL **OR** 42=43)

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## Three-valued logic (example)

**WHERE** 42=43 **OR** (42=**NULL** **OR** 42=43)

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→ False **OR** Unknown

→ Unknown

## Three-valued logic (example)

**WHERE** 42=43 **OR** (42=NULL **OR** 42=43)

→ False **OR** (Unknown **OR** False)

→ False **OR** Unknown

→ Unknown

**WHERE** 42=45 **OR** (42=NULL **OR** 42=42)

## Three-valued logic (example)

**WHERE** 42=43 **OR** (42=NULL **OR** 42=43)

→ False **OR** (Unknown **OR** False)

→ False **OR** Unknown

→ Unknown

**WHERE** 42=45 **OR** (42=NULL **OR** 42=42)

→ False **OR** (Unknown **OR** True)

## Three-valued logic (example)

**WHERE** 42=43 **OR** (42=**NULL** **OR** 42=43)

→ False **OR** (Unknown **OR** False)

→ False **OR** Unknown

→ Unknown

**WHERE** 42=45 **OR** (42=**NULL** **OR** 42=42)

→ False **OR** (Unknown **OR** True)

→ False **OR** True

## Three-valued logic (example)

**WHERE** 42=43 **OR** (42=**NULL** **OR** 42=43)

→ False **OR** (Unknown **OR** False)

→ False **OR** Unknown

→ Unknown

**WHERE** 42=45 **OR** (42=**NULL** **OR** 42=42)

→ False **OR** (Unknown **OR** True)

→ False **OR** True

→ True

# Three-valued logic (AND table)

<b>AND</b>	True	False
True	True	False
False	False	False



# Three-valued logic (AND table)

AND	True	False	NULL
True	True	False	
False	False	False	
NULL			

# Three-valued logic (AND table)

AND	True	False	NULL
True	True	False	
False	False	False	False
NULL		False	

# Three-valued logic (AND table)

AND	True	False	NULL
True	True	False	NULL
False	False	False	False
NULL	NULL	False	NULL

# Three-valued logic (OR table)

OR	True	False
True	True	True
False	True	False

# Three-valued logic (OR table)

OR	True	False	NULL
True	True	True	
False	True	False	
NULL			

# Three-valued logic (OR table)

OR	True	False	NULL
True	True	True	True
False	True	False	
NULL	True		

# Three-valued logic (OR table)

OR	True	False	NULL
True	True	True	True
False	True	False	NULL
NULL	True	NULL	NULL

# Three-valued logic (traps)

- What is `NULL * 42`?



# Three-valued logic (traps)

- What is `NULL * 42`?  
→ `NULL`

## Three-valued logic (traps)

- What is `NULL * 42`?  
→ `NULL`
- What is `NULL / 0`?

# Three-valued logic (traps)

- What is `NULL * 42`?
  - `NULL`
- What is `NULL / 0`?
  - Implementation-dependent: `NULL` or `error`

## Three-valued logic (traps)

- What is `NULL * 42`?  
→ `NULL`
- What is `NULL / 0`?  
→ Implementation-dependent: `NULL` or `error`
- What is `NULL = NULL`?

# Three-valued logic (traps)

- What is `NULL * 42`?  
→ `NULL`
- What is `NULL / 0`?  
→ Implementation-dependent: `NULL` or `error`
- What is `NULL = NULL`?  
→ `NULL`

## Three-valued logic (traps)

- What is `NULL * 42`?  
→ `NULL`
- What is `NULL / 0`?  
→ Implementation-dependent: `NULL` or `error`
- What is `NULL = NULL`?  
→ `NULL`
- What does the following do?  
`SELECT * FROM Book WHERE room=NULL`

## Three-valued logic (traps)

- What is `NULL * 42`?  
→ `NULL`
- What is `NULL / 0`?  
→ Implementation-dependent: `NULL` or `error`
- What is `NULL = NULL`?  
→ `NULL`
- What does the following do?  
`SELECT * FROM Book WHERE room=NULL`  
→ Returns an `empty result`

## Three-valued logic (traps)

- What is `NULL * 42`?  
→ `NULL`
- What is `NULL / 0`?  
→ Implementation-dependent: `NULL` or error
- What is `NULL = NULL`?  
→ `NULL`
- What does the following do?  
`SELECT * FROM Book WHERE room=NULL`  
→ Returns an empty result
- What does the following do?  
`SELECT * FROM Book WHERE room='C42' OR room<>'C42'`



## Three-valued logic (traps)

- What is `NULL * 42`?  
→ `NULL`
- What is `NULL / 0`?  
→ Implementation-dependent: `NULL` or error
- What is `NULL = NULL`?  
→ `NULL`
- What does the following do?  
`SELECT * FROM Book WHERE room=NULL`  
→ Returns an empty result
- What does the following do?  
`SELECT * FROM Book WHERE room='C42' OR room<>'C42'`  
→ Return everything where room is not `NULL`

# Three-valued logic (fixes)

- IS NULL

→ test if an expression is NULL

- Law of **excluded fourth**:

[COND] IS TRUE OR [COND] IS FALSE OR [COND] IS NULL

## Three-valued logic (more complaints)

This is **silly** in terms of semantics!

Book			
date	teacher	class	room
2015-12-07	Antoine	UDM	NULL

```
SELECT * FROM Book WHERE room='C42' OR room<>'C42'
```

## Three-valued logic (more complaints)

This is **silly** in terms of semantics!

Book			
date	teacher	class	room
2015-12-07	Antoine	UDM	NULL

**SELECT** \* **FROM** Book **WHERE** room='C42' **OR** room<>'C42'

Possible worlds:

- **Either** the **NULL** is 'C42'
- ... **or** the **NULL** is something else

## Three-valued logic (more complaints)

This is **silly** in terms of semantics!

Book			
date	teacher	class	room
2015-12-07	Antoine	UDM	NULL

**SELECT** \* **FROM** Book **WHERE** room='C42' **OR** room<>'C42'

Possible worlds:

- **Either** the **NULL** is 'C42'
  - ... **or** the **NULL** is something else
- ... **so** the tuple should **match** in either case!

# Three-valued logic (more traps!)

## Book

<b>date</b>	<b>teacher</b>	<b>class</b>	<b>room</b>
2015-11-23	Antoine	UDM	C47
2015-11-30	Antoine	UDM	C017
2015-12-03	Antoine	UDM	NULL

## Three-valued logic (more traps!)

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date	teacher	class	room
2015-11-23	Antoine	UDM	C47
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### Repairs

room	cause
C42	lavatory leak
NULL	leopard

## Three-valued logic (more traps!)

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date	teacher	class	room
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Repairs

room	cause
C42	lavatory leak
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```
SELECT * FROM Book WHERE room NOT IN
(SELECT room FROM Repairs)
```



## Three-valued logic (more traps!)

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date	teacher	class	room
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→ Empty result!

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```
SELECT * FROM Book WHERE room NOT IN
  (SELECT room FROM Repairs)
```

→ Empty result!

```
SELECT * FROM Book WHERE room NOT IN
  (SELECT room FROM Repairs WHERE room IS NOT NULL)
```

## Three-valued logic (more traps!)

Book				Repairs	
date	teacher	class	room	room	cause
2015-11-23	Antoine	UDM	C47	C42	lavatory leak
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```
SELECT * FROM Book WHERE room NOT IN
  (SELECT room FROM Repairs)
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→ Empty result!

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SELECT * FROM Book WHERE room NOT IN
  (SELECT room FROM Repairs WHERE room IS NOT NULL)
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→ Does **not** contain the **NULL** for 2015-12-03

## Three-valued logic (more traps!)

Book				Repairs	
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```
SELECT * FROM Book WHERE room NOT IN
  (SELECT room FROM Repairs)
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→ Empty result!

```
SELECT * FROM Book WHERE room NOT IN
  (SELECT room FROM Repairs WHERE room IS NOT NULL)
```

→ Does **not** contain the **NULL** for 2015-12-03

```
SELECT * FROM Book WHERE
  (room IN (SELECT room FROM Repairs) IS NOT TRUE)
```

## Even more traps with NULLs

```
SELECT * FROM R NATURAL JOIN S
```

## Even more traps with NULLs

```
SELECT * FROM R NATURAL JOIN S
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→ NULLs will never join

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SELECT * FROM R NATURAL JOIN S
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SELECT a FROM R UNION SELECT a FROM S
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## Even more traps with NULLs

`SELECT * FROM R NATURAL JOIN S`

→ NULLs will **never** join

`SELECT a FROM R UNION SELECT a FROM S`

→ multiple NULLs will **not** be kept



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**SELECT DISTINCT a FROM R**

## Even more traps with NULLs

**SELECT \* FROM R NATURAL JOIN S**

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# Even, even more traps about **NULLs**

## Even, even more traps about NULLs

```
SELECT COUNT(*) FROM R
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SELECT COUNT(*) FROM R
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SELECT COUNT(a) FROM R
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SELECT COUNT(a) FROM R
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→ NULLs will be ignored!

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**SELECT COUNT(\*) FROM R**

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**SELECT COUNT(a) FROM R**

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**SELECT SUM(a) FROM R**



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SELECT COUNT(\*) FROM R

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SELECT AVG(a), SUM(a)/COUNT(\*) FROM R

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→ NULLs will be ignored!

**SELECT SUM(a) FROM R**

→ NULLs will be ignored

**SELECT AVG(a), SUM(a)/COUNT(\*) FROM R**

→ values may differ

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- 1 SQL
- 2 Semantics**
- 3 V-tables
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# Semantics

- We fix a **signature**  $\sigma$ :
  - relation **names**
  - associated **arity**
- We define **uncertain interpretations** for each relation

# Uncertain relation

- An **uncertain relation**: set of **possible worlds**

# Uncertain relation

- An uncertain relation: set of possible worlds

Booking			Booking			Booking			...
date	tch	room	date	tch	room	date	tch	room	...
23	A.	a	23	A.	b	23	A.	c	

# Relational algebra

- Extend relational algebra operators to **uncertain relations**
- The **possible worlds** of the **result** should be...
  - take all **possible worlds** of the inputs
  - apply the operation and get a **possible output**



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Booking

---

23 A. a

---

Booking

---

23 A. b

---

Booking

---

23 A. c

---

⋮

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Booking

23	A.	a
----	----	---

Booking

23	A.	b
----	----	---

U

Booking

23	A.	c
----	----	---

⋮

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<u>Booking</u>		<u>Booking</u>
23   A.   a		30   a   C017

<u>Booking</u>	∪	<u>Booking</u>
23   A.   b		30   b   C017

<u>Booking</u>		<u>Booking</u>
23   A.   c		30   c   C017

⋮		⋮
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<u>Booking</u>		<u>Booking</u>	
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⋮		⋮	
---	--	---	--

# Relational algebra

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$\vdots$		$\vdots$		$\vdots$							

# Representation system

Tables with **NULL** are a **representation** of uncertain tables

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Booking

---

23	A.	NULL
----	----	------

---

# Representation system

Tables with **NULL** are a **representation** of uncertain tables

**Booking**

23	A.	<b>NULL</b>
----	----	-------------

stands for



# Representation system

Tables with **NULL** are a **representation** of uncertain tables

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		⋮												

## Back to the silly example

### Book

date	teacher	class	room
2015-12-07	Antoine	UDM	NULL
2015-12-14	Silviu	UDM	C47

```
SELECT * FROM Book WHERE teacher='Antoine' AND
(room='C42' OR room<>'C42')
```

## Back to the silly example

Book

date	teacher	class	room
2015-12-07	Antoine	UDM	NULL
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```
SELECT * FROM Book WHERE teacher='Antoine' AND
(room='C42' OR room<>'C42')
```

→ How to **represent** the result?

## Representing the output

---

07	A.	UDM	NULL
14	S.	UDM	C47

---

## Representing the output

07	A.	UDM	NULL
14	S.	UDM	C47

represents

# Representing the output

07	A.	UDM	NULL
14	S.	UDM	C47

represents

07	A.	UDM	a	07	A.	UDM	b	07	A.	UDM	C42	...
14	S.	UDM	C47	14	S.	UDM	C47	14	S.	UDM	C47	

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```
SELECT * FROM Book WHERE teacher='A.' AND
      (room='C42' OR room<>'C42')
```

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07	A.	UDM	NULL
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07	A.	UDM	a	07	A.	UDM	b	07	A.	UDM	C42	...
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SELECT * FROM Book WHERE teacher='A.' AND
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```

07	A.	UDM	a	07	A.	UDM	b	07	A.	UDM	C42	...
----	----	-----	---	----	----	-----	---	----	----	-----	-----	-----



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07	A.	UDM	a	07	A.	UDM	b	07	A.	UDM	C42	...
----	----	-----	---	----	----	-----	---	----	----	-----	-----	-----

represented as

## Representing the output

07	A.	UDM	NULL
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07	A.	UDM	a	07	A.	UDM	b	07	A.	UDM	C42	...
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```
SELECT * FROM Book WHERE teacher='A.' AND
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```

07	A.	UDM	a	07	A.	UDM	b	07	A.	UDM	C42	...
----	----	-----	---	----	----	-----	---	----	----	-----	-----	-----

represented as

07	A.	UDM	NULL
----	----	-----	------

# Representation system definition

Uncertain instance: set of possible worlds

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**Uncertain instance:** set of possible worlds

**Uncertainty framework:** concise way to represent uncertain instances

- Here, **Codd tables**

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## Definition (Strong representation system)

For any query in the language,

# Representation system definition

**Uncertain instance:** set of possible worlds

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- Here, **Codd tables**

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## Definition (Strong representation system)

For any query in the language,  
on uncertain instances represented in the framework,

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- Here, **Codd tables**

**Query language:** here, relational algebra

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For any query in the language,  
on uncertain instances represented in the framework,  
the uncertain instance obtained by evaluating the query



# Representation system definition

**Uncertain instance:** set of possible worlds

**Uncertainty framework:** concise way to represent uncertain instances

- Here, **Codd tables**

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## Definition (Strong representation system)

For any query in the language,  
on uncertain instances represented in the framework,  
the uncertain instance obtained by evaluating the query  
can also be represented in the framework.

# Representation system definition

**Uncertain instance:** set of possible worlds

**Uncertainty framework:** concise way to represent uncertain instances

- Here, **Codd tables**

**Query language:** here, relational algebra

## Definition (Strong representation system)

For any query in the language, on uncertain instances represented in the framework, the uncertain instance obtained by evaluating the query can also be represented in the framework.

→ Are Codd tables a **strong representation system**?

# Are Codd tables a representation system?

## Member

id	class
1	UDM
2	UDM
3	IE

## Booking

date	teacher	class	room
2015-12-07	Antoine	UDM	NULL

# Are Codd tables a representation system?

Member		Booking			
id	class	date	teacher	class	room
1	UDM				
2	UDM	2015-12-07	Antoine	UDM	NULL
3	IE				

Can we represent **Member** ⋈ **Booking**?

# Are Codd tables a representation system?

Member		Booking			
id	class	date	teacher	class	room
1	UDM				
2	UDM	2015-12-07	Antoine	UDM	NULL
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Can we represent **Member** ⋈ **Booking**?

Member ⋈ Booking				
id	date	teacher	class	room
1	2015-12-07	Antoine	UDM	NULL
2	2015-12-07	Antoine	UDM	NULL

# Are Codd tables a representation system?

Member		Booking			
id	class	date	teacher	class	room
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Can we represent **Member** ⋈ **Booking**?

Member ⋈ Booking				
id	date	teacher	class	room
1	2015-12-07	Antoine	UDM	NULL
2	2015-12-07	Antoine	UDM	NULL

→ Can you spot the **problem**?

# Multiple values

- When querying Codd tables, we may **duplicate** **NULLs**
- We cannot represent that two **NULLs** are the **same**
- This may cause **problems!**

## Multiple values example

Booking			
date	teacher	class	room
2015-12-07	Antoine	UDM	NULL
2015-12-14	Silviu	UDM	C47

$$\Pi_{\text{room}}(\text{Booking}) - \Pi_{\text{room}}(\sigma_{\text{teacher}=\text{"Antoine"}}(\text{Booking}))$$



## Multiple values example

Booking			
date	teacher	class	room
2015-12-07	Antoine	UDM	NULL
2015-12-14	Silviu	UDM	C47

$$\Pi_{\text{room}}(\text{Booking}) - \Pi_{\text{room}}(\sigma_{\text{teacher}=\text{"Antoine"}}(\text{Booking}))$$

According to SQL

---

According to semantics

---

C47

---

## Multiple values example

Booking			
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2015-12-07	Antoine	UDM	NULL
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According to SQL

---

According to semantics

---

C47

---

But if we try to represent intermediate expressions?

## Multiple values example

Booking			
date	teacher	class	room
2015-12-07	Antoine	UDM	NULL
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$$\Pi_{\text{room}}(\text{Booking}) - \Pi_{\text{room}}(\sigma_{\text{teacher}=\text{"Antoine"}}(\text{Booking}))$$

According to SQL

According to semantics

C47

But if we try to represent intermediate expressions?

$\Pi_{\text{room}}(\text{Booking})$

NULL

C47

$\Pi_{\text{room}}(\sigma_{\text{teacher}=\text{"Antoine"}}(\text{Booking}))$

NULL

# Table of contents

- 1 SQL
- 2 Semantics
- 3 V-tables**
- 4 c-tables

# v-tables

- Idea: give each **NULL** its **own name**  
→ **named NULLs**
- Initially, all **NULLs** are **distinct**
- Propagate their **identities**

# v-tables

- Idea: give each **NULL** its **own name**  
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- Initially, all **NULLs** are **distinct**
- Propagate their **identities**

Member		Booking			
id	class	date	teacher	class	room
1	UDM				
2	UDM	2015-12-07	NULL <sub>1</sub>	UDM	NULL <sub>2</sub>
3	IE				

# v-tables

- Idea: give each **NULL** its own name  
→ named **NULLs**
- Initially, all **NULLs** are **distinct**
- Propagate their **identities**

Member		Booking			
id	class	date	teacher	class	room
1	UDM				
2	UDM	2015-12-07	NULL <sub>1</sub>	UDM	NULL <sub>2</sub>
3	IE				

Member ⋈ Booking					
id	date	teacher	class	room	
1	2015-12-07	NULL <sub>1</sub>	UDM	NULL <sub>2</sub>	
2	2015-12-07	NULL <sub>1</sub>	UDM	NULL <sub>2</sub>	

# v-table semantics

1	2015-12-07	NULL <sub>1</sub>	UDM	NULL <sub>2</sub>
2	2015-12-07	NULL <sub>1</sub>	UDM	NULL <sub>2</sub>



# v-table semantics

1	2015-12-07	NULL <sub>1</sub>	UDM	NULL <sub>2</sub>
2	2015-12-07	NULL <sub>1</sub>	UDM	NULL <sub>2</sub>
1	2015-12-07	aa	UDM	bb
2	2015-12-07	aa	UDM	bb

## v-table semantics

1	2015-12-07	NULL <sub>1</sub>	UDM	NULL <sub>2</sub>
2	2015-12-07	NULL <sub>1</sub>	UDM	NULL <sub>2</sub>
1	2015-12-07	aa	UDM	bb
2	2015-12-07	aa	UDM	bb
1	2015-12-07	ccc	UDM	ddd
2	2015-12-07	ccc	UDM	ddd

## v-table semantics

1	2015-12-07	NULL <sub>L1</sub>	UDM	NULL <sub>L2</sub>
2	2015-12-07	NULL <sub>L1</sub>	UDM	NULL <sub>L2</sub>
1	2015-12-07	aa	UDM	bb
2	2015-12-07	aa	UDM	bb
1	2015-12-07	ccc	UDM	ddd
2	2015-12-07	ccc	UDM	ddd
1	2015-12-07	e	UDM	e
2	2015-12-07	e	UDM	e

# Are v-tables a representation system?

## Member

id	class
1	UDM
2	UDM
3	NULL <sub>0</sub>

## Booking

date	teacher	class	room
2015-12-07	NULL <sub>1</sub>	UDM	NULL <sub>2</sub>

# Are v-tables a representation system?

## Member

id	class
1	UDM
2	UDM
3	NULL <sub>0</sub>

## Booking

date	teacher	class	room
2015-12-07	NULL <sub>1</sub>	UDM	NULL <sub>2</sub>

## Member ⋈ Booking

id	date	teacher	class	room
1	2015-12-07	NULL <sub>1</sub>	UDM	NULL <sub>2</sub>
2	2015-12-07	NULL <sub>1</sub>	UDM	NULL <sub>2</sub>
3	2015-12-07	NULL <sub>1</sub>	UDM	NULL <sub>2</sub>

*if NULL<sub>0</sub> is "UDM"*

# Problem

- v-tables cannot represent **optional rows**
  - the number of rows is **certain**

# Problem

- v-tables cannot represent **optional rows**
  - the number of rows is **certain**
- When **selection**, **join** applies to a **NULL**:
  - we do not know **how to evaluate**
  - we are **uncertain** about whether the tuple matches

# Problem

- v-tables cannot represent **optional rows**
    - the number of rows is **certain**
  - When **selection, join** applies to a **NULL**:
    - we do not know **how to evaluate**
    - we are **uncertain** about whether the tuple matches
- Add **conditions** to rows!



# Condition example

$$R := \Pi_{id, room} (\text{Member} \bowtie \text{Booking})$$

id	room	condition
1	NULL <sub>2</sub>	
2	NULL <sub>2</sub>	
3	NULL <sub>2</sub>	if NULL <sub>0</sub> is "UDM"

Rooms

room	seats
C42	20
NULL <sub>3</sub>	25

## Condition example

$$R := \Pi_{id, room}(\text{Member} \bowtie \text{Booking})$$

id	room	condition
1	NULL <sub>2</sub>	
2	NULL <sub>2</sub>	
3	NULL <sub>2</sub>	if NULL <sub>0</sub> is "UDM"

Rooms

room	seats
C42	20
NULL <sub>3</sub>	25

$R \bowtie \text{Rooms}$

id	room	seats	condition
----	------	-------	-----------

# Condition example

$$R := \Pi_{id, room} (\text{Member} \bowtie \text{Booking})$$

id	room	condition
1	$NULL_2$	
2	$NULL_2$	
3	$NULL_2$	if $NULL_0$ is "UDM"

Rooms

room	seats
C42	20
$NULL_3$	25

$R \bowtie \text{Rooms}$

id	room	seats	condition
1	$NULL_2$	20	if $NULL_2 = \text{"C42"}$
1	$NULL_2$	25	if $NULL_2 = NULL_3$

# Condition example

$$R := \Pi_{id, room} (\text{Member} \bowtie \text{Booking})$$

id	room	condition
1	$NULL_2$	
2	$NULL_2$	
3	$NULL_2$	if $NULL_0$ is "UDM"

## Rooms

room	seats
C42	20
$NULL_3$	25

$$R \bowtie \text{Rooms}$$

id	room	seats	condition
1	$NULL_2$	20	if $NULL_2 = \text{"C42"}$
1	$NULL_2$	25	if $NULL_2 = NULL_3$
2	$NULL_2$	20	if $NULL_2 = \text{"C42"}$
2	$NULL_2$	25	if $NULL_2 = NULL_3$

# Condition example

$$R := \Pi_{id, room} (\text{Member} \bowtie \text{Booking})$$

id	room	condition
1	$NULL_2$	
2	$NULL_2$	
3	$NULL_2$	if $NULL_0$ is "UDM"

## Rooms

room	seats
C42	20
$NULL_3$	25

## $R \bowtie \text{Rooms}$

id	room	seats	condition
1	$NULL_2$	20	if $NULL_2 = \text{"C42"}$
1	$NULL_2$	25	if $NULL_2 = NULL_3$
2	$NULL_2$	20	if $NULL_2 = \text{"C42"}$
2	$NULL_2$	25	if $NULL_2 = NULL_3$
3	$NULL_2$	20	if $NULL_2 = \text{"C42"}$ and $NULL_0 = \text{"UDM"}$
3	$NULL_2$	25	if $NULL_2 = NULL_3$ and $NULL_0 = \text{"UDM"}$

# Table of contents

- 1 SQL
- 2 Semantics
- 3 V-tables
- 4 c-tables**

# c-tables

- Named **NULLs**, plus **conditions** on tuples
- Conditions can use:

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  - **true**
  - **false**



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# c-tables

- Named **NULLs**, plus **conditions** on tuples
- Conditions can use:
  - **true**
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  - $NULL_i = NULL_j$
  - $NULL_i = \text{"value"}$
  - **Boolean** operators

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- Named **NULLs**, plus **conditions** on tuples
- Conditions can use:
  - **true**
  - **false**
  - $\text{NULL}_i = \text{NULL}_j$
  - $\text{NULL}_i = \text{"value"}$
  - **Boolean** operators

→ Are **c-tables** a **strong representation system**?

# Relational algebra operators: product

<b>S</b>	
<b>s</b>	<i>condition</i>
$s_1$	$C_1$
$s_2$	$C_2$

# Relational algebra operators: product

<span style="color: red;">S</span>		<span style="color: red;">T</span>	
<b>s</b>	<i>condition</i>	<b>t</b>	<i>condition</i>
$s_1$	$C_1$	$t_1$	$D_1$
$s_2$	$C_2$	$t_2$	$D_2$

# Relational algebra operators: product

S		T	
s	<i>condition</i>	t	<i>condition</i>
$s_1$	$C_1$	$t_1$	$D_1$
$s_2$	$C_2$	$t_2$	$D_2$

$S \times T$		
s	t	<i>condition</i>

# Relational algebra operators: product

<b>S</b>		<b>T</b>	
<b>s</b>	<i>condition</i>	<b>t</b>	<i>condition</i>
$s_1$	$C_1$	$t_1$	$D_1$
$s_2$	$C_2$	$t_2$	$D_2$

<b>S</b> × <b>T</b>		
<b>s</b>	<b>t</b>	<i>condition</i>
$s_1$	$t_1$	$C_1$ and $D_1$
$s_1$	$t_2$	$C_1$ and $D_2$
$s_2$	$t_1$	$C_2$ and $D_1$
$s_2$	$t_2$	$C_2$ and $D_2$



# Relational algebra operators: union

<span style="color: red;">S</span>	
<b>s</b>	<i>condition</i>
$s_0$	$C_0$
$s_1$	$C_1$

# Relational algebra operators: union

S		S2	
<b>s</b>	<i>condition</i>	<b>s</b>	<i>condition</i>
$s_0$	$C_0$	$s_0$	$D_0$
$s_1$	$C_1$	$s_2$	$D_2$

# Relational algebra operators: union

<b>S</b>		<b>S2</b>	
<b>s</b>	<i>condition</i>	<b>s</b>	<i>condition</i>
$s_0$	$C_0$	$s_0$	$D_0$
$s_1$	$C_1$	$s_2$	$D_2$

<b>S</b> $\cup$ <b>S2</b>	
<b>s</b>	<i>condition</i>

# Relational algebra operators: union

<b>S</b>		<b>S2</b>	
<b>s</b>	<i>condition</i>	<b>s</b>	<i>condition</i>
$s_0$	$C_0$	$s_0$	$D_0$
$s_1$	$C_1$	$s_2$	$D_2$

<b>S <math>\cup</math> S2</b>	
<b>s</b>	<i>condition</i>
$s_0$	$C_0$ or $D_0$
$s_1$	$C_1$
$s_2$	$D_2$

# Relational algebra operators: project

S

<b>s</b>	<b>t</b>	<i>condition</i>
$s_0$	$t_0$	$C_0$
$s_0$	$t_1$	$C_1$
$s_2$	$t_2$	$C_2$

# Relational algebra operators: project

**S**

<b>s</b>	<b>t</b>	<i>condition</i>
$s_0$	$t_0$	$C_0$
$s_0$	$t_1$	$C_1$
$s_2$	$t_2$	$C_2$

$\Pi_s(S)$

<b>s</b>	<i>condition</i>
----------	------------------

# Relational algebra operators: project

**S**

<b>s</b>	<b>t</b>	<i>condition</i>
$s_0$	$t_0$	$C_0$
$s_0$	$t_1$	$C_1$
$s_2$	$t_2$	$C_2$

$\Pi_s(S)$

<b>s</b>	<i>condition</i>
$s_0$	$C_0$ or $C_1$
$s_2$	$C_2$

# Relational algebra operators: select (1)

S

<b>s</b>	<b>t</b>	<i>condition</i>
42	$t_0$	$C_0$
43	$t_1$	$C_1$
NULL <sub><i>j</i></sub>	$t_2$	$C_2$



# Relational algebra operators: select (1)

S

s	t	condition
42	$t_0$	$C_0$
43	$t_1$	$C_1$
NULL <sub>j</sub>	$t_2$	$C_2$

$\sigma_{s="42"}(S)$

s	t	condition
---	---	-----------

# Relational algebra operators: select (1)

S

s	t	condition
42	$t_0$	$C_0$
43	$t_1$	$C_1$
NULL <sub>j</sub>	$t_2$	$C_2$

$\sigma_{s="42"}(S)$

s	t	condition
42	$t_0$	$C_0$

# Relational algebra operators: select (1)

S

s	t	condition
42	$t_0$	$C_0$
43	$t_1$	$C_1$
NULL <sub>j</sub>	$t_2$	$C_2$

$\sigma_{s="42"}(S)$

s	t	condition
42	$t_0$	$C_0$
NULL <sub>j</sub>	$t_2$	

# Relational algebra operators: select (1)

S

s	t	condition
42	$t_0$	$C_0$
43	$t_1$	$C_1$
$NULL_j$	$t_2$	$C_2$

$\sigma_{s="42"}(S)$

s	t	condition
42	$t_0$	$C_0$
$NULL_j$	$t_2$	$C_2$ and $NULL_j = "42"$

# Relational algebra operators: select (2)

S

<b>s</b>	<b>t</b>	<i>condition</i>
42	42	$C_0$
43	42	$C_1$
$NULL_j$	42	$C_2$
42	$NULL_j$	$C_3$
$NULL_p$	$NULL_q$	$C_4$

# Relational algebra operators: select (2)

S

<b>s</b>	<b>t</b>	<i>condition</i>
42	42	$C_0$
43	42	$C_1$
$NULL_j$	42	$C_2$
42	$NULL_j$	$C_3$
$NULL_p$	$NULL_q$	$C_4$

$\sigma_{s=t}(S)$

<b>s</b>	<b>t</b>	<i>condition</i>
----------	----------	------------------

# Relational algebra operators: select (2)

S

<b>s</b>	<b>t</b>	<i>condition</i>
42	42	$C_0$
43	42	$C_1$
$NULL_j$	42	$C_2$
42	$NULL_j$	$C_3$
$NULL_p$	$NULL_q$	$C_4$

$\sigma_{s=t}(S)$

<b>s</b>	<b>t</b>	<i>condition</i>
42	42	

# Relational algebra operators: select (2)

S

<b>s</b>	<b>t</b>	<i>condition</i>
42	42	$C_0$
43	42	$C_1$
$NULL_j$	42	$C_2$
42	$NULL_j$	$C_3$
$NULL_p$	$NULL_q$	$C_4$

$\sigma_{s=t}(S)$

<b>s</b>	<b>t</b>	<i>condition</i>
42	42	$C_0$



# Relational algebra operators: select (2)

S

s	t	condition
42	42	$C_0$
43	42	$C_1$
$NULL_j$	42	$C_2$
42	$NULL_j$	$C_3$
$NULL_p$	$NULL_q$	$C_4$

$\sigma_{s=t}(S)$

s	t	condition
42	42	$C_0$
$NULL_j$	42	

# Relational algebra operators: select (2)

S

s	t	condition
42	42	$C_0$
43	42	$C_1$
$NULL_i$	42	$C_2$
42	$NULL_j$	$C_3$
$NULL_p$	$NULL_q$	$C_4$

$\sigma_{s=t}(S)$

s	t	condition
42	42	$C_0$
$NULL_i$	42	$C_2$ and $NULL_i = "42"$

# Relational algebra operators: select (2)

S

s	t	condition
42	42	$C_0$
43	42	$C_1$
$NULL_i$	42	$C_2$
42	$NULL_j$	$C_3$
$NULL_p$	$NULL_q$	$C_4$

$\sigma_{s=t}(S)$

s	t	condition
42	42	$C_0$
$NULL_i$	42	$C_2$ and $NULL_i = "42"$
42	$NULL_j$	

# Relational algebra operators: select (2)

S

s	t	condition
42	42	$C_0$
43	42	$C_1$
$NULL_i$	42	$C_2$
42	$NULL_j$	$C_3$
$NULL_p$	$NULL_q$	$C_4$

$\sigma_{s=t}(S)$

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42	42	$C_0$
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---

42  $(NULL_i = "42" \text{ and } NULL_j = "42") \text{ or } ((NULL_k = NULL_j \text{ or } NULL_j = "43") \text{ and } (NULL_i = NULL_j))$

---

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We can represent the **output** of a query as a c-table

Member ⋈ Booking

id	date	teacher	class	room
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→ All **intractable** in general

# Credits

Thanks to Pierre Senellart for useful feedback.



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