



# Uncertain Data Management Open-World Query Answering

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# Table of contents

Basics

Contexts

Languages

Chase

Advanced topics

# Incompleteness

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- The **true** state of the world is  $W$
- We **may have**  $I \neq W$

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- $I$  may be **complete**:  $W \subseteq I$

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  - $I$  may be **complete**:  $W \subseteq I$
- Today,  $I$  is **correct** but not **complete**

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  - We **want**: evaluate  $Q$  on  $W$
  - We **don't have**  $W$
- What can we do?!

## Constraints to the rescue!

- We know that  $I \subseteq W$  (correct)
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## Definition (Open-World Query Answering – OWQA)

Given an instance  $I$ , Boolean CQ  $Q$ , and constraints  $\Theta$ , decide whether all  $W \supseteq I$  that satisfy  $\Theta$  also satisfy  $Q$ .

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**Combined complexity.** Input is  $I, \Theta, Q$

**Data complexity.** Input is  $I$

## Example

Relation **Class** in *I*

<b>date</b>	<b>teacher</b>	<b>resp</b>	<b>name</b>	<b>num</b>
2016-11-28	Antoine	Fabian	Uncert. Data Mgmt	2
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**Book** in *I*

<b>date</b>	<b>room</b>	<b>prof</b>
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“Every class has a booking.”

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*“Every class has a booking.”*

$Q : \exists t r \mathbf{Book}(\text{“2016-11-28”, } t, r)$

*“Is there a room booked on Nov 28th?”*

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- $\Theta$  and  $Q$  are usually **different** languages...



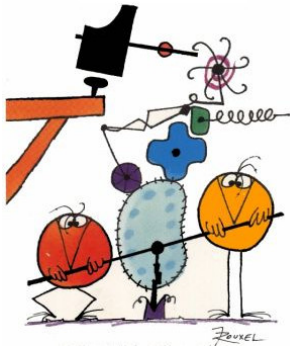
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- $I$  is where we want to **scale**
- $\Theta$  and  $Q$  are usually **different** languages...
- ... if we express both in the **same** language, it will be hard to achieve good **complexities**! (or even **decidability**...)



# Repairing the database

## Class

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## Constraints:

- The **responsible** for a class must teach **some** class
  - Every class must have a **first** session
- What can we **deduce**?

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## Constraints:

- The **responsible** for a class must teach **some** class
  - Every class must have a **first** session
- What can we **deduce**?
- **Q** is true iff it is true on **all** completions

## But why deal with broken databases?

- The data may have come from a **different source**
- The constraints may have been imposed **after the fact**
- User input may be **incorrect**
- You want a **resilient** system...

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Date	créneau	Type	Sigle	Titre de l'activité pédagogique	Groupe	Equipe enseignante	Salle
27/10/2015	13:30 - 16:45	Leçon	INF922	ISC651 Technologies Applicatives	1	Jean DUPONT	C47
03/11/2015	09:00 - 12:00	Leçon	INF922	Integration d'applications (EAI, SOA) Ph Bron	1	⚠	C46
03/11/2015	13:30 - 16:45	Leçon	INF922	ISC651 Cloud Computing Ph Bron;	1	⚠	C46
	08:30			INF922: ingénierie des			

# Reasoning (AI)

- Artificial **reasoning**: draw **consequences** from what you know
  - $I$  contains the **facts**
  - $\Theta$  are the **reasoning rules**
  - $Q$  is what we want to **figure out**

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    - $I$  contains the **facts**
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    - $Q$  is what we want to **figure out**
- Can we **deduce**  $Q$  from  $I$  using  $\Theta$ ?
- Is  $Q$  **certain** to hold?

# Data integration

- $I$  contains  $I_1, \dots, I_n$ , the course databases of all D&K schools
- We want to create a virtual **global** database  $I$  of classes

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## Class1

date	name
2016-11-28	UDM
2016-12-05	UDM
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**Class**

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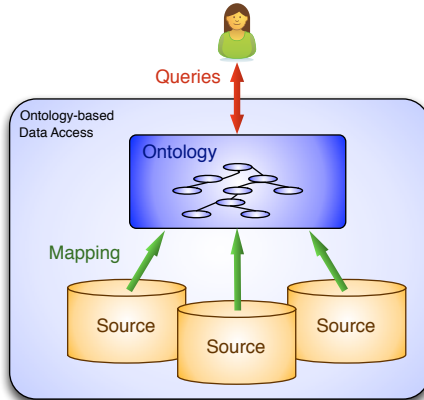
date	name
2016-11-28	UDM
2016-12-05	UDM
2016-12-12	UDM
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**Class**

date	teacher	resp	name	num
2016-11-28	?	?	UDM	?
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2016-12-12	?	?	UDM	?
2017-01-14	?	?	UDM	?

# Ontology-based data access

- In general: use a **common** schema for reasoning
- $I$  contains heterogeneous **data sources**
- $\Theta$  describes **mappings** from sources to common schema and **reasoning rules** and **constraints** on the common schema
- $Q$  is the **query** posed the common schema



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# First-order logic

All **constraints** for  $\Theta$  are in **first-order logic** (FO):

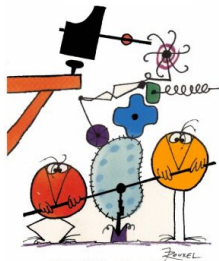
- contains **atoms**  $R(x, y, z)$
- closed under Boolean AND, OR, NOT
- existential quantification  $\exists x \phi(x)$
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→ **Why not just use FO for constraints then?!**



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Given an input FO formula  $\Theta$ , is it **satisfiable**?  
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- Proof: Encode a tiling system, or  
encode transition rules for a Turing machine

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					...
					...
⋮	⋮	⋮	⋮	⋮	⋮


















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→ We consider **weaker languages**

					...
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# Tuple-generating dependencies

Tuple-generating dependencies (TGDs), classical database rules:

$$\forall \mathbf{x} \, Q'(\mathbf{x}) \Rightarrow \exists \mathbf{y} \, Q''(\mathbf{x}, \mathbf{y})$$

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**Useful for:**

- **Integrity constraints:** see above
- **Schema mappings:** copy facts from  $I_1$  to  $I$
- **Reasoning:**  $\forall x \, \text{Human}(x) \Rightarrow \text{Mortal}(x)$

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from [Chandra et al., 1981, Beeri and Vardi, 1981]

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    - from [Chandra et al., 1981, Beeri and Vardi, 1981]
- We need **less expressive** languages

# Inclusion dependencies

**Inclusion dependencies** (IDs), classical database rules:

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The TGD example was in fact **also an ID**:

$$\begin{aligned} \forall \text{date, prof, } r, n, i, \text{ Class}(\text{date, prof, } r, n, i) \Rightarrow \\ \exists \text{room, Book}(\text{date, room, prof}) \end{aligned}$$

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- We will study other decidable classes of TGDs



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## Chase example

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Book

date	room	prof
2016-12-05	?1	Antoine
2016-12-12	?2	Antoine

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  - TGD  $\forall \mathbf{x} Q'(\mathbf{x}) \Rightarrow \exists \mathbf{y} Q''(\mathbf{x}, \mathbf{y})$
  - find **a** such that  $Q'(\mathbf{a})$  but not  $Q''(\mathbf{a}, \mathbf{b})$  for any **b**



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- **Create** new elements  $\mathbf{b}$
- **Create** new facts to make  $Q'(\mathbf{a}, \mathbf{b})$  true

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  - **Create** new elements  $\mathbf{b}$
  - **Create** new facts to make  $Q'(\mathbf{a}, \mathbf{b})$  true
- Take the **infinite result** of this process

# Infinite chase example

$$\forall t u \text{ Mentor}(t, u) \Rightarrow \exists s \text{ Mentor}(s, t)$$

Mentor	
master	padawan

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master	padawan
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# Infinite chase example

$$\forall t u \text{ Mentor}(t, u) \Rightarrow \exists s \text{ Mentor}(s, t)$$

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## Theorem

For any instance  $I$ , TGDs  $\Theta$ , Boolean CQ  $Q$ ,  
the following are **equivalent**:

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- How to **reason** about this infinite chase?

# Chase termination

- Sometimes, the chase of  $I$  by  $\Theta$  is **finite**
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- When is the chase **finite**?

# Full dependencies

- If no TGD has an  $\exists$ , then the chase is **finite**  
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# Full dependencies

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- **Good:**  $\forall d, r, p \text{ Book}(d, r, p) \Rightarrow \text{Room}(r)$
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- **Bad**:  $\forall \mathbf{x} \text{ Mentor}(\mathbf{x}) \Rightarrow \exists \mathbf{y} \text{ Mentor}(\mathbf{x}, \mathbf{y})$
- More general **acyclicity conditions**

# Infinite chase

- What can we do if the chase is **infinite**?
- **Bounded derivation depth**: we can **truncate** the chase:
  - we fix  $\Theta$  and look at the **size** of  $Q$
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# Infinite chase

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where  $Q$  can be made true
- **Bounded treewidth**: the chase is like a **tree**:
  - we can reason about **infinite** and **regular** trees
  - use **tree automata**, following Courcelle's theorem
  - some rules preserve this, e.g., the **guarded fragments**

# Table of contents

Basics

Contexts

Languages

Chase

Advanced topics

# Query rewriting

- The **chase**: reason about **consequences** of  $I$  under  $\Theta$
- Other option: reason about **how to prove**  $Q$



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$$Q_2 : \exists \text{prof, r, n, i, } \text{Class}(\text{"2016-11-28", prof, r, n, i})$$

# Query rewriting and inclusion dependencies

- To show that OWQA for **inclusion dependencies** is decidable...

$$\forall \mathbf{x} A'(\mathbf{x}) \Rightarrow \exists \mathbf{y} A''(\mathbf{x}, \mathbf{y})$$

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- Rewrite all atoms in the query in **all possible ways**
  - Each atom rewritten by **only one atom**
  - The query size does not **increase**
- Replace  $Q$  by a **union** of conjunctive queries
  - OWQA for IDs is **decidable**
  - OWQA for IDs has **tractable** data complexity

- TGDs cannot express **everything**

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# Description logics

- **TGDs** cannot express **everything**

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- **Disjunction**: if  $A$  then  $B$  or  $C$
  - **Negation**: you **cannot** have both  $A$  and  $B$
- **Description logics**: expressive rules
- signature must have **arity** at most 2

## Description logics (2)

- Description logics have a specific **syntax**

Teacher  $\sqsubseteq$  Prof  $\sqcap (\exists \text{Advisor}^- . \text{Prof})$

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Languages	UNA	Complexity		
		Combined complexity Satisfiability	Data complexity	
			Instance checking	Query answering
$DL\text{-}Lite_{core}^{[H]}$ $DL\text{-}Lite_{horn}^{[H]}$ $DL\text{-}Lite_{krom}^{[H]}$ $DL\text{-}Lite_{bool}^{[H]}$	yes/no	$NLOGSPACE \geq [A]$ $P \leq [Th.8.2] \geq [A]$ $NLOGSPACE \leq [Th.8.2]$ $NP \leq [Th.8.2] \geq [A]$	$in AC^0$ $in AC^0$ $in AC^0$ $in AC^0 \leq [Th.8.3]$	$in AC^0$ $in AC^0 \leq [C]$ $coNP \geq [B]$ $coNP$
$DL\text{-}Lite_{core}^{[F][N](\mathcal{HF})(\mathcal{HN})}$ $DL\text{-}Lite_{horn}^{[F][N](\mathcal{HF})(\mathcal{HN})}$ $DL\text{-}Lite_{krom}^{[F][N](\mathcal{HF})(\mathcal{HN})}$ $DL\text{-}Lite_{bool}^{[F][N](\mathcal{HF})(\mathcal{HN})}$	yes	$NLOGSPACE$ $P \leq [Th.5.8, 5.13]$ $NLOGSPACE \leq [Th.5.7, 5.13]$ $NP \leq [Th.5.6, 5.13]$	$in AC^0$ $in AC^0$ $in AC^0$ $in AC^0 \leq [Cor.6.2]$	$in AC^0$ $in AC^0 \leq [Th.7.1]$ $coNP$ $coNP$
$DL\text{-}Lite_{core/horn}^{[F](\mathcal{HF})}$ $DL\text{-}Lite_{krom}^{[F](\mathcal{HF})}$ $DL\text{-}Lite_{bool}^{[F](\mathcal{HF})}$ $DL\text{-}Lite_{core/horn}^{[N](\mathcal{HN})}$ $DL\text{-}Lite_{krom/bool}^{[N](\mathcal{HN})}$	no	$P \leq [Cor.8.8] \geq [Th.8.7]$ $P \leq [Cor.8.8]$ $NP$ $NP \geq [Th.8.4]$ $NP \leq [Th.8.5]$	$P \geq [Th.8.7]$ $P$ $P \leq [Cor.8.8]$ $coNP \geq [Th.8.4]$ $coNP$	$P$ $coNP$ $coNP$ $coNP$ $coNP$
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# Equality-generating dependencies

- Another important constraint for  $\Theta$ : **functional dependencies**
  - There can't be **two bookings** for one room at the same time
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- Another important constraint for  $\Theta$ : **functional dependencies**
  - There can't be **two bookings** for one room at the same time
  - There can't be **two rooms** for one session
- Functional dependencies can be **added** to  $\Theta$  for OWQA
  - **Decidable** for description logics
  - **Undecidable** with inclusion dependencies

## Definition (Open-World Query Answering – OWQA)

Given an instance  $I$ , Boolean CQ  $Q$ , and constraints  $\Theta$ , decide whether all  $W \supseteq I$  that satisfy  $\Theta$  satisfy  $Q$ .

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- Shouldn't we **reflect** this?



## Definition (Finite Open-World Query Answering – FOWQA)

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- The world  $W$  is actually **finite**
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- If the **chase** is infinite, it no longer works
- Imposing finiteness may make a **difference**

→ Very **hard** to reason about FOWQA!

# Partial completeness

- We have assumed that  $I$  was **incomplete**
- Sometimes, we know **which relations** are complete
  - e.g., the list of **rooms** may be **complete**
  - the list of **classes** may be **incomplete**

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  - If I know the lecturer of a class, then I know **all lecturers**
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→ **Partial completeness assumption** [Galárraga et al., 2013]

# Slide credits

- Slide 34:  
<http://www.slideshare.net/MartnRezk/slides-swat4-ls>,  
slide 17, licence CC-BY-SA 3.0<sup>1</sup>
- Slides 16 and 36: Jaques Rouxel, *Les Shadoks* (*reproduit en vertu du droit de citation*)
- Slide 34: [Artale et al., 2009], p 18

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<sup>1</sup><http://creativecommons.org/licenses/by-sa/3.0/>


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