

Uncertain Data Management Relational Probabilistic Database Models

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Uncertain instances

Remember from **last class**:

- Fix a finite set of **possible tuples** of same arity
- A **possible world**: a subset of the **possible tuples**
- An **uncertain relation**: set of **possible worlds**

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<i>U₁</i>			<i>U₂</i>		
date	teacher	room	date	teacher	room
04	Silviu	C017	04	Silviu	C017
04	Antoine	C017	04	Antoine	C017
04	Antoine	C47	04	Antoine	C47
11	Silviu	C017	11	Silviu	C017
11	Silviu	C47	11	Silviu	C47
11	Antoine	C017	11	Antoine	C017

Probabilistic instances

- **Support** \mathcal{U} : uncertain relation

Probabilistic instances

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- Probability distribution π on \mathcal{U} :

Probabilistic instances

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 - **Function** from \mathcal{U} to reals in $[0, 1]$
 - It must **sum up** to 1: $\sum_{I \in \mathcal{U}} \pi(I) = 1$

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\mathcal{U}_1			\mathcal{U}_2		
date	teacher	room	date	teacher	room
04	Silviu	C017	04	Silviu	C017
04	Antoine	C017	04	Antoine	C017
04	Antoine	C47	04	Antoine	C47
11	Silviu	C017	11	Silviu	C017
11	Silviu	C47	11	Silviu	C47
11	Antoine	C017	11	Antoine	C017

Probabilistic instances

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U_1			U_2		
date	teacher	room	date	teacher	room
04	Silviu	C017	04	Silviu	C017
04	Antoine	C017	04	Antoine	C017
04	Antoine	C47	04	Antoine	C47
11	Silviu	C017	11	Silviu	C017
11	Silviu	C47	11	Silviu	C47
11	Antoine	C017	11	Antoine	C017

$\pi(U_1) = 0.8$

$\pi(U_2) = 0.2$

What about NULLs?

Remember that last time we saw:

- Codd-tables and v-tables and c-tables, with NULLs
- Boolean c-tables, with NULLs only in conditions
→ Boolean variables

What about NULLs?

Remember that last time we saw:

- Codd-tables and v-tables and c-tables, with NULLs
 - Boolean c-tables, with NULLs only in conditions
 - Boolean variables
- We focus for probabilities on models like Boolean c-tables
- Easier to define probabilities on a finite space!

Relational algebra on uncertain instances

Remember from **last class**:

- Extend relational algebra operators to **uncertain instances**
- The **possible worlds** of the **result** should be...
 - take all **possible worlds** in the supports of the inputs
 - apply the operation and get the **possible outputs**

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U_1

04	S.	C017
11	S.	C47

U_2

11	A.	C017
----	----	------

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U_1		
04	S.	C017
11	S.	C47

 \cup

U_2		
11	A.	C017

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U_1				V_1		
04	S.	C017	∪	_____		
11	S.	C47		_____		
U_2				V_2		
11	A.	C017		_____	11	A. C017
_____				_____		

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U_1		V_1	
04 S. C017	∪		=
11 S. C47			

U_2		V_2
11 A. C017		11 A. C017

Relational algebra on uncertain instances

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U_1		V_1		V_2	
04 S. C017 11 S. C47	∪		=	04 S. C017 11 S. C47	
11 A. C017		11 A. C017		11 A. C017 11 A. C017	

Relational algebra on probabilistic instances

- Let's adapt relational algebra to **probabilistic instances**
- The **possible worlds** of the **result** should be...

Relational algebra on probabilistic instances

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Relational algebra on probabilistic instances

- Let's adapt relational algebra to **probabilistic instances**
- The **possible worlds** of the **result** should be...
 - take all **possible worlds** of the inputs
 - apply the operation and get a **possible output**
- The **probability** of each possible world should be...
 - consider **all input possible worlds** that give it
 - sum up their **probabilities**

Example of relational algebra on probabilistic instances

Example of relational algebra on probabilistic instances

 U_1

04	S.	C017
11	S.	C47

 U_2

11	A.	C017
----	----	------

Example of relational algebra on probabilistic instances

 U_1

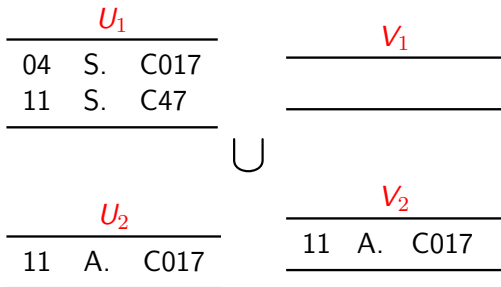
04	S.	C017
11	S.	C47

U

 U_2

11	A.	C017
----	----	------

Example of relational algebra on probabilistic instances



Example of relational algebra on probabilistic instances

U_1		V_1
04 S. C017		
11 S. C47		
$\pi(U_1) = 0.8$	\cup	$\pi(V_1) = 0.9$
U_2		V_2
11 A. C017		11 A. C017
$\pi(U_2) = 0.2$		$\pi(V_2) = 0.1$

Example of relational algebra on probabilistic instances

$$\begin{array}{c}
 \overline{U_1} \\
 04 \quad S. \quad C017 \\
 11 \quad S. \quad C47 \\
 \hline
 \pi(U_1) = 0.8
 \end{array}
 \cup
 \begin{array}{c}
 \overline{V_1} \\
 \hline
 \hline
 \pi(V_1) = 0.9
 \end{array}
 =
 \begin{array}{c}
 \overline{U_2} \\
 11 \quad A. \quad C017 \\
 \hline
 \pi(U_2) = 0.2
 \end{array}
 \begin{array}{c}
 \overline{V_2} \\
 11 \quad A. \quad C017 \\
 \hline
 \pi(V_2) = 0.1
 \end{array}$$

Example of relational algebra on probabilistic instances

U_1		
04	S.	C017
11	S.	C47

$\pi(U_1) = 0.8$

 \cup

V_1		
$\pi(V_1) = 0.9$		

 $=$

U_2		
11	A.	C017

$\pi(U_2) = 0.2$

V_2		
11	A.	C017

$\pi(V_2) = 0.1$

W_1		
04	S.	C017
11	S.	C47

Example of relational algebra on probabilistic instances

$$U_1$$

04	S.	C017
11	S.	C47

$$\pi(U_1) = 0.8$$

$$\cup$$

$$V_1$$

--	--	--

$$\pi(V_1) = 0.9$$

$$V_2$$

--	--	--

11	A.	C017
----	----	------

$$\pi(V_2) = 0.1$$

$$=$$

$$W_1$$

04	S.	C017
11	S.	C47

$$W_2$$

04	S.	C017
11	S.	C47
11	A.	C017

$$U_2$$

11	A.	C017
----	----	------

$$\pi(U_2) = 0.2$$

Example of relational algebra on probabilistic instances

$$U_1$$

04	S.	C017
11	S.	C47

$$\pi(U_1) = 0.8$$

$$\cup$$

$$U_2$$

11	A.	C017
----	----	------

$$\pi(U_2) = 0.2$$

$$V_1$$

--	--	--

$$\pi(V_1) = 0.9$$

$$V_2$$

--	--	--

11	A.	C017
----	----	------

$$\pi(V_2) = 0.1$$

$$=$$

$$W_1$$

04	S.	C017
11	S.	C47

$$W_2$$

04	S.	C017
11	S.	C47
11	A.	C017

$$W_3$$

11	A.	C017
----	----	------

Example of relational algebra on probabilistic instances

$$U_1$$

04	S.	C017
11	S.	C47

$$\pi(U_1) = 0.8$$

$$\cup$$

$$U_2$$

11	A.	C017
----	----	------

$$\pi(U_2) = 0.2$$

$$V_1$$

--	--	--

$$\pi(V_1) = 0.9$$

$$V_2$$

11	A.	C017
----	----	------

$$\pi(V_2) = 0.1$$

$$=$$

$$W_1$$

04	S.	C017
11	S.	C47

$$\pi(W_1) = 0.8 \cdot 0.9$$

$$W_2$$

04	S.	C017
11	S.	C47
11	A.	C017

$$W_3$$

11	A.	C017
----	----	------

Example of relational algebra on probabilistic instances

$$U_1$$

04	S.	C017
11	S.	C47

$$\pi(U_1) = 0.8$$

$$\cup$$

$$V_1$$

--	--	--

$$\pi(V_1) = 0.9$$

$$V_2$$

11	A.	C017
----	----	------

$$\pi(V_2) = 0.1$$

$$=$$

$$W_1$$

04	S.	C017
11	S.	C47

$$\pi(W_1) = 0.8 \cdot 0.9$$

$$W_2$$

04	S.	C017
11	S.	C47
11	A.	C017

$$\pi(W_2) = 0.8 \cdot 0.1$$

$$W_3$$

11	A.	C017
----	----	------

Example of relational algebra on probabilistic instances

$$U_1$$

04	S.	C017
11	S.	C47

$$\pi(U_1) = 0.8$$

$$\cup$$

$$V_1$$

--	--	--

$$\pi(V_1) = 0.9$$

$$V_2$$

--	--	--

11	A.	C017
----	----	------

$$\pi(V_2) = 0.1$$

$$U_2$$

11	A.	C017
----	----	------

$$\pi(U_2) = 0.2$$

$$=$$

$$W_1$$

04	S.	C017
11	S.	C47

$$\pi(W_1) = 0.8 \cdot 0.9$$

$$W_2$$

04	S.	C017
11	S.	C47
11	A.	C017

$$\pi(W_1) = 0.8 \cdot 0.1$$

$$W_3$$

11	A.	C017
----	----	------

$$\pi(W_1) = 0.2 \cdot 0.9$$

Example of relational algebra on probabilistic instances

$$U_1$$

04	S.	C017
11	S.	C47

$$\pi(U_1) = 0.8$$

$$\cup$$

$$V_1$$

--	--	--

$$\pi(V_1) = 0.9$$

$$V_2$$

11	A.	C017
----	----	------

$$\pi(V_2) = 0.1$$

$$=$$

$$W_1$$

04	S.	C017
11	S.	C47

$$\pi(W_1) = 0.8 \cdot 0.9$$

$$W_2$$

04	S.	C017
11	S.	C47
11	A.	C017

$$\pi(W_1) = 0.8 \cdot 0.1$$

$$W_3$$

11	A.	C017
----	----	------

$$\pi(W_1) = 0.2 \cdot 0.9 + 0.2 \cdot 0.1$$

Representation system

- Remember that if we have N possible tuples

Representation system

- Remember that if we have N possible tuples
→ there are 2^N possible instances

Representation system

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Representation system

- Remember that if we have N possible tuples
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 - there are 2^{2^N} possible uncertain instances
 - **writing out** an uncertain instance is **exponential**
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- For **probabilistic instances**:
 - there are **infinitely many** possible instances
 - **writing out** a probabilistic instance is still **exponential**

Representation system

- Remember that if we have N possible tuples
 - there are 2^N possible instances
 - there are 2^{2^N} possible uncertain instances
 - **writing out** an uncertain instance is **exponential**
- Last time we saw **Boolean c-tables** as a **concise way** to **represent** uncertain instances
- For **probabilistic instances**:
 - there are **infinitely many** possible instances
 - **writing out** a probabilistic instance is still **exponential**
- How to **represent** probabilistic instances?

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Tuple-independent databases

- The **simplest** model: tuple-independent databases
- Annotate each **instance fact** with a **probability**

Tuple-independent databases

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 U

date	teacher	room
04	Silviu	C017
04	Antoine	C017
11	Silviu	C017

Tuple-independent databases

- The **simplest** model: tuple-independent databases
- Annotate each **instance fact** with a **probability**

 U

date	teacher	room	
04	Silviu	C017	0.8
04	Antoine	C017	0.2
11	Silviu	C017	1

Semantics of TID

- Each tuple is **kept** or **discarded** with the probability
- Probabilistic choices are **independent** across tuples

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U

date	teacher	room	
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04	Antoine	C017	0.2
11	Silviu	C017	1

U

date	teacher	room
------	---------	------

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U

date	teacher	room	
04	Silviu	C017	0.8
04	Antoine	C017	0.2
11	Silviu	C017	1

U

date	teacher	room
04	Silviu	C017

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U

date	teacher	room	
04	Silviu	C017	0.8
04	Antoine	C017	0.2
11	Silviu	C017	1

U

date	teacher	room
04	Silviu	C017
04	Antoine	C017

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04	Silviu	C017	0.8
04	Antoine	C017	0.2
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date	teacher	room
04	Silviu	C017
04	Antoine	C017
11	Silviu	C017

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<i>U</i>				<i>U</i>		
date	teacher	room		date	teacher	room
04	Silviu	C017	0.8	04	Silviu	C017
04	Antoine	C017	0.2	04	Antoine	C017
11	Silviu	C017	1	11	Silviu	C017

What's the **probability** of this outcome?

Semantics of TID

- Each tuple is **kept** or **discarded** with the probability
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<i>U</i>				<i>U</i>		
date	teacher	room		date	teacher	room
04	Silviu	C017	0.8	04	Silviu	C017
04	Antoine	C017	0.2	04	Antoine	C017
11	Silviu	C017	1	11	Silviu	C017

What's the **probability** of this outcome?

0.8

Semantics of TID

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<i>U</i>				<i>U</i>		
date	teacher	room		date	teacher	room
04	Silviu	C017	0.8	04	Silviu	C017
04	Antoine	C017	0.2	04	Antoine	C017
11	Silviu	C017	1	11	Silviu	C017

What's the **probability** of this outcome?

$$0.8 \times$$

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<i>U</i>							<i>U</i>		
date	teacher	room		date	teacher	room			
04	Silviu	C017	0.8	04	Silviu	C017			
04	Antoine	C017	0.2	04	Antoine	C017			
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What's the **probability** of this outcome?

$$0.8 \times (1 - 0.2)$$

Semantics of TID

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- Probabilistic choices are **independent** across tuples

<i>U</i>				<i>U</i>		
date	teacher	room		date	teacher	room
04	Silviu	C017	0.8	04	Silviu	C017
04	Antoine	C017	0.2	04	Antoine	C017
11	Silviu	C017	1	11	Silviu	C017

What's the **probability** of this outcome?

$$0.8 \times (1 - 0.2) \times 1$$

Getting a probability distribution

The **semantics** of a TID instance is a **probabilistic instance**...
→ the **possible worlds** are the subsets

Getting a probability distribution

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Formally, for a TID instance I , the **probability** of J :

Getting a probability distribution

The **semantics** of a TID instance is a **probabilistic instance**...

→ the **possible worlds** are the subsets

→ always keeping tuples with **probability 1**

Formally, for a TID instance I , the **probability** of J :

- we must have $J \subseteq I$
- product of p_t for each tuple t **kept** in J
- product of $1 - p_t$ for each tuple t **not kept** in J

Is it a probability distribution?

Do the probabilities always **sum to 1**?

Is it a probability distribution?

Do the probabilities always **sum to 1**?

- **0 tuples:** vacuous

Is it a probability distribution?

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- **1 tuple:** $p + (1 - p) = 1$

Is it a probability distribution?

Do the probabilities always **sum to 1**?

- **0 tuples:** vacuous
- **1 tuple:** $p + (1 - p) = 1$
- **2 tuples:** $p_1 p_2 + p_1(1 - p_2) + (1 - p_1)p_2 + (1 - p_1)(1 - p_2)$

Is it a probability distribution?

Do the probabilities always **sum to 1**?

- **0 tuples:** vacuous
- **1 tuple:** $p + (1 - p) = 1$
- **2 tuples:** $p_1 p_2 + p_1(1 - p_2) + (1 - p_1)p_2 + (1 - p_1)(1 - p_2)$
→ $p_1(p_2 + (1 - p_2)) + (1 - p_1)(p_2 + (1 - p_2))$

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Do the probabilities always **sum to 1**?

- **0 tuples:** vacuous
- **1 tuple:** $p + (1 - p) = 1$
- **2 tuples:** $p_1 p_2 + p_1(1 - p_2) + (1 - p_1)p_2 + (1 - p_1)(1 - p_2)$
 - $p_1(p_2 + (1 - p_2)) + (1 - p_1)(p_2 + (1 - p_2))$
 - $(p_1 + (1 - p_1))(p_2 + (1 - p_2))$

Is it a probability distribution?

Do the probabilities always **sum to 1**?

- **0 tuples:** vacuous
- **1 tuple:** $p + (1 - p) = 1$
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 - $p_1(p_2 + (1 - p_2)) + (1 - p_1)(p_2 + (1 - p_2))$
 - $(p_1 + (1 - p_1))(p_2 + (1 - p_2))$
 - $p_2 + (1 - p_2)$

Is it a probability distribution?

Do the probabilities always **sum to 1**?

- **0 tuples:** vacuous
- **1 tuple:** $p + (1 - p) = 1$
- **2 tuples:** $p_1 p_2 + p_1(1 - p_2) + (1 - p_1)p_2 + (1 - p_1)(1 - p_2)$
 - $p_1(p_2 + (1 - p_2)) + (1 - p_1)(p_2 + (1 - p_2))$
 - $(p_1 + (1 - p_1))(p_2 + (1 - p_2))$
 - $p_2 + (1 - p_2)$
- **More tuples:** $p_1(\dots) + (1 - p_1)(\dots)$ and **induction hypothesis**

Strong representation system

Remember from **last class**:

Uncertain instance: set of possible worlds

Strong representation system

Remember from **last class**:

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Uncertainty framework: concise way to represent uncertain instances

Strong representation system

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Uncertainty framework: concise way to represent uncertain instances

Query language: here, relational algebra

Strong representation system

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Definition (Strong representation system)

For any query in the language,

Strong representation system

Remember from **last class**:

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Uncertainty framework: concise way to represent uncertain instances

Query language: here, relational algebra

Definition (Strong representation system)

For any query in the language,
on uncertain instances represented in the framework,

Strong representation system

Remember from **last class**:

Uncertain instance: set of possible worlds

Uncertainty framework: concise way to represent uncertain instances

Query language: here, relational algebra

Definition (Strong representation system)

For any query in the language,
on uncertain instances represented in the framework,
the uncertain instance obtained by evaluating the query

Strong representation system

Remember from **last class**:

Uncertain instance: set of possible worlds

Uncertainty framework: concise way to represent uncertain instances

Query language: here, relational algebra

Definition (Strong representation system)

For any query in the language,
on uncertain instances represented in the framework,
the uncertain instance obtained by evaluating the query
can also be represented in the framework.

Strong representation system

Remember from **last class**:

Uncertain instance: set of possible worlds

Uncertainty framework: concise way to represent uncertain instances

Query language: here, relational algebra

Definition (Strong representation system)

For any query in the language,
on uncertain instances represented in the framework,
the uncertain instance obtained by evaluating the query
can also be represented in the framework.

→ Are TID instances a **strong representation system**?

Implementing select

U

date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2
11	Silviu	C47	1

Implementing select

 U

date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2
11	Silviu	C47	1

 $\sigma_{\text{teacher}=\text{"Silviu"}}(U)$

date	teacher	room
-------------	----------------	-------------

Implementing select

 U

date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2
11	Silviu	C47	1

 $\sigma_{\text{teacher}=\text{"Silviu"}}(U)$

date	teacher	room	
04	Silviu	C47	0.8
11	Silviu	C47	1

Implementing select

 U

date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2
11	Silviu	C47	1

 $\sigma_{\text{teacher}=\text{"Silviu"}}(U)$

date	teacher	room	
04	Silviu	C47	0.8
11	Silviu	C47	1

→ Is this correct?

Implementing select

 U

date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2
11	Silviu	C47	1

 $\sigma_{\text{teacher}=\text{"Silviu"}}(U)$

date	teacher	room	
04	Silviu	C47	0.8
11	Silviu	C47	1

→ Is this correct?

→ So far, so good.

Implementing project

U

date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2
11	Silviu	C47	1
11	Antoine	C47	0.1
18	Silviu	C47	0.9

Implementing project

 U

date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2
11	Silviu	C47	1
11	Antoine	C47	0.1
18	Silviu	C47	0.9

 $\pi_{\text{date}}(U)$

date

Implementing project

 U

date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2
11	Silviu	C47	1
11	Antoine	C47	0.1
18	Silviu	C47	0.9

 $\pi_{\text{date}}(U)$

date

04
11
18

Implementing project

 U

date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2
11	Silviu	C47	1
11	Antoine	C47	0.1
18	Silviu	C47	0.9

 $\pi_{\text{date}}(U)$

date	
04	
11	
18	0.9

Implementing project

 U

date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2
11	Silviu	C47	1
11	Antoine	C47	0.1
18	Silviu	C47	0.9

 $\pi_{\text{date}}(U)$

date	
04	
11	1
18	0.9

Implementing project

 U

date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2
11	Silviu	C47	1
11	Antoine	C47	0.1
18	Silviu	C47	0.9

 $\pi_{\text{date}}(U)$

date	
04	$1 - (1 - 0.2) \cdot (1 - 0.8)$
11	1
18	0.9

Implementing project

 U

date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2
11	Silviu	C47	1
11	Antoine	C47	0.1
18	Silviu	C47	0.9

 $\pi_{\text{date}}(U)$

date	
04	$1 - (1 - 0.2) \cdot (1 - 0.8)$
11	1
18	0.9

→ Is this correct?

Implementing project

 U

date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2
11	Silviu	C47	1
11	Antoine	C47	0.1
18	Silviu	C47	0.9

 $\pi_{\text{date}}(U)$

date	
04	$1 - (1 - 0.2) \cdot (1 - 0.8)$
11	1
18	0.9

- Is this correct?
- So far, so good

Implementing product

U

date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2

Implementing product

U

date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2

Repair

room	cause
C47	leopard 0.1

Implementing product

U

date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2

Repair

room	cause
C47	leopard 0.1

U × Repair

date	teacher	room	cause
------	---------	------	-------

Implementing product

 U

date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2

Repair

room	cause
C47	leopard 0.1

 $U \times \text{Repair}$

date	teacher	room	cause
04	Silviu	C47	leopard
04	Antoine	C47	leopard

Implementing product

 U

date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2

Repair

room	cause
C47	leopard 0.1

 $U \times \text{Repair}$

date	teacher	room	cause	
04	Silviu	C47	leopard	0.8×0.1
04	Antoine	C47	leopard	0.2×0.1

Implementing product

 U

date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2

Repair

room	cause
C47	leopard 0.1

 $U \times \text{Repair}$

date	teacher	room	cause	
04	Silviu	C47	leopard	0.8×0.1
04	Antoine	C47	leopard	0.2×0.1

→ Is this correct?

Implementing product ... OR NOT!

 U

date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2

Repair

room	cause
C47	leopard 0.1

 $U \times \text{Repair}$

date	teacher	room	cause	
04	Silviu	C47	leopard	0.8×0.1
04	Antoine	C47	leopard	0.2×0.1

→ Is this **correct**?→ It's **WRONG!**

Why is it wrong?

U

date	teacher	room	
04	Silviu	C47	1
04	Antoine	C47	1

Why is it wrong?

U

date	teacher	room	
04	Silviu	C47	1
04	Antoine	C47	1

Repair

room	cause
C47	leopard 1/2

Why is it wrong?

 U

date	teacher	room	
04	Silviu	C47	1
04	Antoine	C47	1

Repair

room	cause
C47	leopard 1/2

 $U \times \text{Repair}$

date	teacher	room	cause
04	Silviu	C47	leopard
04	Antoine	C47	leopard

Why is it wrong?

 U

date	teacher	room	
04	Silviu	C47	1
04	Antoine	C47	1

Repair

room	cause
C47	leopard 1/2

 $U \times \text{Repair}$

date	teacher	room	cause	
04	Silviu	C47	leopard	1/2
04	Antoine	C47	leopard	1/2

Why is it wrong?

U				Repair	
date	teacher	room		room	cause
04	Silviu	C47	1	C47	leopard 1/2
04	Antoine	C47	1		

$U \times \text{Repair}$					
date	teacher	room		cause	
04	Silviu	C47		leopard	1/2
04	Antoine	C47		leopard	1/2

- The two tuples are **not independent!**
- The first is there **iff** the second is there.

Why does it matter?

$U \times \text{Repair}$

date	teacher	room	cause	
04	Silviu	C47	leopard	1/2
04	Antoine	C47	leopard	1/2

Why does it matter?

$U \times \text{Repair}$

date	teacher	room	cause	
04	Silviu	C47	leopard	1/2
04	Antoine	C47	leopard	1/2

$\pi_{\text{room}}(U \times \text{Repair})$

room
C47

Why does it matter?

$U \times \text{Repair}$

date	teacher	room	cause	
04	Silviu	C47	leopard	1/2
04	Antoine	C47	leopard	1/2

$\pi_{\text{room}}(U \times \text{Repair})$

room	
C47	$1 - (1 - 1/2) \times (1 - 1/2)$

Why does it matter?

$U \times \text{Repair}$

date	teacher	room	cause	
04	Silviu	C47	leopard	1/2
04	Antoine	C47	leopard	1/2

$\pi_{\text{room}}(U \times \text{Repair})$

room	
C47	$1 - (1 - 1/2) \times (1 - 1/2)$

→ Probability of 3/4...

Why does it matter?

$U \times \text{Repair}$

date	teacher	room	cause	
04	Silviu	C47	leopard	1/2
04	Antoine	C47	leopard	1/2

$\pi_{\text{room}}(U \times \text{Repair})$

room	
C47	$1 - (1 - 1/2) \times (1 - 1/2)$

→ Probability of 3/4...

→ But the leopard had probability 1/2!

TID are not a strong representation system

- Remember how **Codd tables** required **named nulls**?
 - The result of a query on TID may **not** be a TID
- We will see that the correlations can be **complex**

TID are not a strong representation system

- Remember how **Codd tables** required **named nulls**?
- The result of a query on TID may **not** be a TID
- We will see that the correlations can be **complex**

- How to **evaluate** queries on a TID then?
- List all **possible worlds** and count the probabilities

Query evaluation done right

U

date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2

Query evaluation done right

U

date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2

Repair

room	cause	
C47	leopard	0.1

Query evaluation done right

<i>U</i>			
date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2

<i>Repair</i>	
room	cause
C47	leopard 0.1

$$\pi_{\text{room}}(U \times \text{Repair})$$

room

C47

Query evaluation done right

<i>U</i>			
date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2

<i>Repair</i>	
room	cause
C47	leopard 0.1

 $\pi_{\text{room}}(U \times \text{Repair})$

room
C47 ???

Query evaluation done right

<i>U</i>			
date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2

<i>Repair</i>		
room	cause	
C47	leopard	0.1

$$\pi_{\text{room}}(U \times \text{Repair})$$

room	
C47	???

- **Either** there is no leopard and then no result...

Query evaluation done right

<i>U</i>			
date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2

<i>Repair</i>		
room	cause	
C47	leopard	0.1

$$\pi_{\text{room}}(U \times \text{Repair})$$

room
C47 ???

- **Either** there is no leopard and then no result...
- **Or** there is a leopard and then...

Query evaluation done right

<i>U</i>			
date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2

<i>Repair</i>		
room	cause	
C47	leopard	0.1

$$\pi_{\text{room}}(U \times \text{Repair})$$

room
C47 ???

- **Either** there is no leopard and then no result...
- **Or** there is a leopard and then...
 - **Non-empty result:**

Query evaluation done right

<i>U</i>			
date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2

Repair		
room	cause	
C47	leopard	0.1

$$\pi_{\text{room}}(U \times \text{Repair})$$

room
C47 ???

- **Either** there is no leopard and then no result...
- **Or** there is a leopard and then...
 - **Non-empty result:** $1 - (1 - 0.8)(1 - 0.2)$

Query evaluation done right

<i>U</i>			
date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2

<i>Repair</i>		
room	cause	
C47	leopard	0.1

$$\pi_{\text{room}}(U \times \text{Repair})$$

room	
C47	???

- **Either** there is no leopard and then no result...
- **Or** there is a leopard and then...
 - **Non-empty result:** $1 - (1 - 0.8)(1 - 0.2) = 0.84$

Query evaluation done right

<i>U</i>			
date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2

<i>Repair</i>	
room	cause
C47	leopard 0.1

$$\pi_{\text{room}}(U \times \text{Repair})$$

room
C47

- **Either** there is no leopard and then no result...
- **Or** there is a leopard and then...
 - **Non-empty result:** $1 - (1 - 0.8)(1 - 0.2) = 0.84$
- The **query probability** is:

Query evaluation done right

<i>U</i>			
date	teacher	room	
04	Silviu	C47	0.8
04	Antoine	C47	0.2

<i>Repair</i>	
room	cause
C47	leopard 0.1

$$\pi_{\text{room}}(U \times \text{Repair})$$

room	
C47	0.084

- **Either** there is no leopard and then no result...
- **Or** there is a leopard and then...
 - **Non-empty result:** $1 - (1 - 0.8)(1 - 0.2) = 0.84$
- The **query probability** is: 0.1×0.84

Expressiveness of TID

Can we represent **all** probabilistic instances with TID?

Expressiveness of TID

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*“The class is taught by Antoine or Silviu or no one but **not both**”*

Expressiveness of TID

Can we represent **all** probabilistic instances with TID?

*“The class is taught by Antoine or Silviu or no one but **not both**”*

U_1

teacher

Silviu

$\pi(U_1) = 0.8$

Expressiveness of TID

Can we represent **all** probabilistic instances with TID?

*“The class is taught by Antoine or Silviu or no one but **not both**”*

U_1	U_2
teacher	teacher
Silviu	Antoine
$\pi(U_1) = 0.8$	$\pi(U_2) = 0.1$

Expressiveness of TID

Can we represent **all** probabilistic instances with TID?

*“The class is taught by Antoine or Silviu or no one but **not both**”*

U_1	U_2	U_3
<hr/> teacher <hr/>	<hr/> teacher <hr/>	<hr/> teacher <hr/>
Silviu	Antoine	
<hr/> $\pi(U_1) = 0.8$ <hr/>	<hr/> $\pi(U_2) = 0.1$ <hr/>	<hr/> $\pi(U_3) = 0.1$ <hr/>

Expressiveness of TID

Can we represent **all** probabilistic instances with TID?

*“The class is taught by Antoine or Silviu or no one but **not both**”*

U_1	U_2	U_3
teacher	teacher	teacher
Silviu	Antoine	
$\pi(U_1) = 0.8$	$\pi(U_2) = 0.1$	$\pi(U_3) = 0.1$

U
teacher
Antoine
Silviu

Expressiveness of TID

Can we represent **all** probabilistic instances with TID?

*“The class is taught by Antoine or Silviu or no one but **not both**”*

U_1	U_2	U_3
teacher	teacher	teacher
Silviu	Antoine	
$\pi(U_1) = 0.8$	$\pi(U_2) = 0.1$	$\pi(U_3) = 0.1$

U
teacher
Antoine 0.1
Silviu

Expressiveness of TID

Can we represent **all** probabilistic instances with TID?

*“The class is taught by Antoine or Silviu or no one but **not both**”*

U_1	U_2	U_3
teacher	teacher	teacher
Silviu	Antoine	
$\pi(U_1) = 0.8$	$\pi(U_2) = 0.1$	$\pi(U_3) = 0.1$

U	
teacher	
Antoine	0.1
Silviu	0.8

Expressiveness of TID

Can we represent **all** probabilistic instances with TID?

*“The class is taught by Antoine or Silviu or no one but **not both**”*

U_1	U_2	U_3
teacher	teacher	teacher
Silviu	Antoine	
$\pi(U_1) = 0.8$	$\pi(U_2) = 0.1$	$\pi(U_3) = 0.1$

U	
teacher	
Antoine	0.1
Silviu	0.8

→ We **cannot** forbid that both teach the class!

Table of contents

- 1 Probabilistic instances
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Block-independent disjoint instances

- A more expressive framework than TID
- Call some attributes the **key** (underlined)

Block-independent disjoint instances

- A more expressive framework than TID
- Call some attributes the **key** (underlined)

 U

<u>mon</u>	<u>day</u>	teacher	room
Jan	04	Silviu	C017
Jan	04	Antoine	C017
Jan	11	Silviu	C47
Jan	11	Antoine	C017

Block-independent disjoint instances

- A **more expressive framework** than TID
- Call some attributes the **key** (underlined)

U

<u>mon</u>	<u>day</u>	teacher	room
Jan	04	Silviu	C017
Jan	04	Antoine	C017
Jan	11	Silviu	C47
Jan	11	Antoine	C017

- The **blocks** are the sets of tuples with the same key

Block-independent disjoint instances

- A **more expressive framework** than TID
- Call some attributes the **key** (underlined)

U

<u>mon</u>	<u>day</u>	teacher	room
Jan	04	Silviu	C017
Jan	04	Antoine	C017
Jan	11	Silviu	C47
Jan	11	Antoine	C017

- The **blocks** are the sets of tuples with the same key
- Each **tuple** has a probability

Block-independent disjoint instances

- A **more expressive framework** than TID
- Call some attributes the **key** (underlined)

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<u>mon</u>	<u>day</u>	teacher	room	
Jan	04	Silviu	C017	0.9
Jan	04	Antoine	C017	0.1
Jan	11	Silviu	C47	0.8
Jan	11	Antoine	C017	0.1

- The **blocks** are the sets of tuples with the same key
- Each **tuple** has a probability

Block-independent disjoint instances

- A **more expressive framework** than TID
- Call some attributes the **key** (underlined)

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<u>mon</u>	<u>day</u>	teacher	room	
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Jan	11	Silviu	C47	0.8
Jan	11	Antoine	C017	0.1

- The **blocks** are the sets of tuples with the same key
- Each **tuple** has a probability
- Probabilities must **sum** to ≤ 1 in each **block**

BID semantics

 U

<u>mon</u>	<u>day</u>	teacher	room	
Jan	04	Silviu	C017	0.9
Jan	04	Antoine	C017	0.1
Jan	11	Silviu	C47	0.8
Jan	11	Antoine	C017	0.1

BID semantics

 U

<u>mon</u>	<u>day</u>	teacher	room	
Jan	04	Silviu	C017	0.9
Jan	04	Antoine	C017	0.1
Jan	11	Silviu	C47	0.8
Jan	11	Antoine	C017	0.1

- For each **block**:

BID semantics

 U

<u>mon</u>	<u>day</u>	teacher	room	
Jan	04	Silviu	C017	0.9
Jan	04	Antoine	C017	0.1
Jan	11	Silviu	C47	0.8
Jan	11	Antoine	C017	0.1

- For each **block**:
 - Pick **one** tuple according to probabilities

BID semantics

 U

<u>mon</u>	<u>day</u>	teacher	room	
Jan	04	Silviu	C017	0.9
Jan	04	Antoine	C017	0.1
Jan	11	Silviu	C47	0.8
Jan	11	Antoine	C017	0.1

- For each **block**:
 - Pick **one** tuple according to probabilities
 - Possibly **no** tuple if probabilities are < 1

BID semantics

 U

<u>mon</u>	<u>day</u>	teacher	room	
Jan	04	Silviu	C017	0.9
Jan	04	Antoine	C017	0.1
Jan	11	Silviu	C47	0.8
Jan	11	Antoine	C017	0.1

- For each **block**:
 - Pick **one** tuple according to probabilities
 - Possibly **no** tuple if probabilities are < 1
- Do choices **independently** in each block

BID semantics

U

<u>mon</u>	<u>day</u>	teacher	room	
Jan	04	Silviu	C017	0.9
Jan	04	Antoine	C017	0.1
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Jan	11	Antoine	C017	0.1

U

<u>mon</u>	<u>day</u>	teacher	room	

- For each **block**:
 - Pick **one** tuple according to probabilities
 - Possibly **no** tuple if probabilities are < 1

→ Do choices **independently** in each block

BID semantics

U

<u>mon</u>	<u>day</u>	teacher	room	
Jan	04	Silviu	C017	0.9
Jan	04	Antoine	C017	0.1
Jan	11	Silviu	C47	0.8
Jan	11	Antoine	C017	0.1

U

<u>mon</u>	<u>day</u>	teacher	room
Jan	04	Silviu	C017
Jan	04	Antoine	C017

- For each **block**:
 - Pick **one** tuple according to probabilities
 - Possibly **no** tuple if probabilities are < 1

→ Do choices **independently** in each block

BID semantics

U

<u>mon</u>	<u>day</u>	teacher	room	
Jan	04	Silviu	C017	0.9
Jan	04	Antoine	C017	0.1
Jan	11	Silviu	C47	0.8
Jan	11	Antoine	C017	0.1

U

<u>mon</u>	<u>day</u>	teacher	room
Jan	04	Silviu	C017
Jan	04	Antoine	C017
Jan	11	Silviu	C47
Jan	11	Antoine	C017

- For each **block**:
 - Pick **one** tuple according to probabilities
 - Possibly **no** tuple if probabilities are < 1

→ Do choices **independently** in each block

BID captures TID

- Each TID can be expressed as a BID...

BID captures TID

- Each **TID** can be expressed as a BID...
 - Take all attributes as **key**
 - Each block contains a **single tuple**

BID captures TID

- Each **TID** can be expressed as a BID...
 - Take all attributes as **key**
 - Each block contains a **single tuple**

U

<u>date</u>	<u>teacher</u>	<u>room</u>	
04	Silviu	C017	0.8
04	Antoine	C017	0.2
11	Silviu	C017	1

Expressiveness of BID

Can we represent **all** probabilistic instances with BID?

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“The class is taught by exactly two among Antoine, Silviu, Fabian.”

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Can we represent **all** probabilistic instances with BID?

“The class is taught by exactly two among Antoine, Silviu, Fabian.”

U_1
teacher
Silviu
Fabian
$\pi(U_1) = 0.8$

Expressiveness of BID

Can we represent **all** probabilistic instances with BID?

“The class is taught by exactly two among Antoine, Silviu, Fabian.”

U_1	U_2
<hr/> teacher <hr/>	<hr/> teacher <hr/>
Silviu	Antoine
Fabian	Fabian
<hr/> $\pi(U_1) = 0.8$	<hr/> $\pi(U_2) = 0.1$

Expressiveness of BID

Can we represent **all** probabilistic instances with BID?

“The class is taught by exactly two among Antoine, Silviu, Fabian.”

U_1	U_2	U_3
teacher	teacher	teacher
Silviu	Antoine	Antoine
Fabian	Fabian	Silviu
$\pi(U_1) = 0.8$	$\pi(U_2) = 0.1$	$\pi(U_3) = 0.1$

Expressiveness of BID

Can we represent **all** probabilistic instances with BID?

“The class is taught by exactly two among Antoine, Silviu, Fabian.”

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- If **teacher** is not a key, then **only one tuple**

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- If **teacher** is a key teacher, then TID
- If **teacher** is not a key, then **only one tuple**
- We **cannot represent** this probabilistic instance as a BID

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- 1 Probabilistic instances
- 2 TID
- 3 BID
- 4 pc-tables**
- 5 Conclusion

Boolean c-tables

Remember **Boolean c-tables**:

- Set of **Boolean variables** x_1, x_2, \dots
- Each **tuple** carries a **condition**
 - **Variables** and **true** and **false**
 - **Boolean operators**

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x_1 Silviu is sick

x_2 Projector in C017 is working

pc-tables

A (Boolean) *pc-table* is a Boolean *c-table*
plus a *probability* p_i for each x_i
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 - Yeah, it's like *TID instances!*

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→ Probability 0.1

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→ Probability 0.2

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- Here: **only** this valuation, 0.18

pc-tables capture TID

Give each tuple its **own** variable:

U

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→ Give each **variable** the **probability** of the tuple

pc-tables capture mutually exclusive

- Remember **non-Boolean** c-tables

pc-tables capture mutually exclusive

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mon	day	teacher	room	
Jan	04	Silviu	C017	$x = 1$
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Reminder: rewriting non-Boolean to Boolean

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Reminder: rewriting non-Boolean to Boolean

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→ How to choose the **probabilities?**

Choosing the probabilities

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Converting mutually exclusive to pc-tables

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- **Rewriting:**

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→ **Rewriting:**

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→ x_1 has proba $1/9$, x_2 has proba $1/2$, x'_2 has proba 0

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x_1 has probability 0.1

y_1 has probability 0.1

y_2 has probability 1/9

Strong representation system

- Remember from last class:
Boolean **c-tables** are a **strong representation system**
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Boolean c-tables are a strong representation system
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- pc-tables are a strong representation system

Capturing all probabilistic instances

- Remember:
 - **Support** \mathcal{U} : uncertain relation
 - Here, set of subsets of a **finite** set of tuples
 - **Probability distribution** π on \mathcal{U}

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→ Can **any** probabilistic instance be **represented** by a pc-table?

Capturing uncertain instances with Boolean c-tables (1)

Remember from **last time**:

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a	d	a	d	a	d	a	d
b	e	b	e	b	e	b	e
c	f	c	f	c	f	c	f

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c	f	c	f	c	f	c	f

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→ We can **also** do this with pc-tables

Capturing uncertain instances with Boolean c-tables (2)

Remember: the **second step** was to **reduce** to binary:

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→ We have **seen this**: this is encoding a **mutually exclusive** choice

Table of contents

- 1 Probabilistic instances
- 2 TID
- 3 BID
- 4 pc-tables
- 5 Conclusion**

Summary

We have seen **relational** formalisms for **probabilistic** instances:

- TID, a simple model with **independent probabilities** on tuples
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- In the next class: how to evaluate **queries** efficiently
 - Let's see a few **advanced topics**

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$x_1 \vee x_2 \vee x_3$	
teacher	
Antoine	x_1
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- **Semantics**: ignore valuations that violate the global condition
- Easier to **add things** to the global condition

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 - Also, **fuzzy databases:** facts can be any intermediate value between true (1) and false (0)
- **Continuous distributions:** impose conditions like “this value follows a normal distribution”
 - Usually **intractable** to reason with
 - **MCDBs:** Monte Carlo DataBases: use **sampling**

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 - Always a **maximal world** for inclusion

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